

## **Wing Keung Wong**

Department of Finance, Fintech Center, and Big Data Research Center,  
Asia University

- The multivariate nonlinear test not only takes into consideration both dependent and joint effects among variables but is also able to detect a multivariate nonlinear deterministic process that cannot be detected by using any linear causality test.
- To overcome this limitation, this paper suggests including cointegration in the analysis.

## **Cointegration**

Johansen cointegration test proposed by Johansen (1988), Johansen and Juselius (1990) and Johansen (1991) as some studies, for example, Gonzalo (1994), confirm that the Johansen cointegration test performs better than the other cointegration tests, namely the ADF test (Engle and Granger, 1987). In addition, when GARCH errors exist in the model, Lee and Tse (1996) conclude that the bias is not too serious when using Johansen's cointegration test if we compare its performance with other cointegration tests

Johansen and Juselius (1990) and Johansen (1991) develop a multivariate maximum likelihood (ML) procedure for the estimation of the cointegrating vectors. According to Johansen's procedure, the  $p$ -dimensional unrestricted Vector Autoregression (VAR) model should be first specified with  $k$  lags:

$$\mathbf{Z}_t = \sum_{i=1}^k \mathbf{A}_i \mathbf{Z}_{t-i} + \Psi \mathbf{D}_t + U_t \quad (1)$$

where  $\mathbf{Z}_t = [M_t, D_t, Y_t]'$  is a  $3 \times 1$  vector of stochastic variables and  $M_t$ ,  $D_t$ , and  $Y_t$  are to be the logarithms of the ratio of bank deposit liabilities to nominal GDP, the ratio of claims on private sector to nominal GDP, and real GDP per capita in period  $t$ , respectively.  $\mathbf{D}_t$  is a vector of dummies and  $\mathbf{A}_i$  is a vector of parameters. This VAR could be rewritten as:

$$\Delta \mathbf{Z}_t = \sum_{i=1}^{k-1} \Phi_i \Delta \mathbf{Z}_{t-i} + \Pi \mathbf{Z}_{t-i} + \Psi \mathbf{D}_t + U_t . \quad (2)$$

The hypothesis of cointegration is formulated as a reduced rank of the  $\Pi$  matrix where  $\Pi = \alpha\beta'$  such that  $\alpha$  is the vector or matrix of the adjustment parameter and  $\beta$  is the vector or matrix of the cointegrating vectors. According to Engle and Granger (1987), if the rank of  $\Pi$  ( $r$ ) is not equal to zero, then  $r$  cointegrating vectors exist. The number of cointegrating vectors is less than or equal to the number of variables, which is 3 in our case. The likelihood ratio (LR) reduced the rank test for the null hypothesis of at most  $r$  cointegrating vectors is given by the following Trace statistic, and for the null hypothesis of  $r$  against the alternative of  $r+1$  cointegrating vectors is known as the maximal eigenvalue statistic

$$\begin{aligned}
3\lambda_{trace} &= -T \sum_{i=r}^m \ln(1 - \lambda_{i+1}) , \quad \lambda_{max} \\
&= -T \ln(1 - \lambda_{r+1}) \quad (3)
\end{aligned}$$

where  $m$  is the maximum number of possible cointegrating vectors which is 3 in our case, in this paper,  $r = 0, 1, 2$  and  $\lambda_1 > \lambda_2 > \lambda_3$  denote eigenvalues of their corresponding eigenvectors  $v = (v_1, v_2, v_3)$ . If the null hypothesis of  $r$  cointegrating vectors is accepted, then the rank of the  $\Pi$  matrix equal to  $r$  and there is exactly  $r$  cointegrating vector.

## Granger Causality

Since our analysis presented in next section (see Table 1) confirms that all the variables  $M_t$ ,  $D_t$ , and  $Y_t$  are I(1), academics and practitioners are interested in testing whether there is any causality relationship among the differences of the variables  $M_t$ ,  $D_t$ , and  $Y_t$ . We let  $m_t = \Delta M_t$ ,  $d_t = \Delta D_t$ , and  $y_t = \Delta Y_t$ . This means that academics and practitioners are interested in testing whether there is any causality relationship among  $m_t$ ,  $d_t$ , and  $y_t$ . Thus, in this paper we will test whether there is any linear Granger causality and thereafter examine whether there is any nonlinear Granger causality among the variables  $m_t$ ,  $d_t$ , and  $y_t$ .

## *Linear Granger Causality*

To test the linear causality relationship between two vectors of stationary time series, we set  $x_t = (x_{1,t}, \dots, x_{n_1,t})'$  and  $y_t = (y_{1,t}, \dots, y_{n_2,t})'$  say  $x_t = (m_t, d_t)'$  and  $y_t = (y_t)'$ , where there are 3 series in total. Under this setting, one could construct the following vector autoregressive regression (VAR) model:

$$\begin{pmatrix} x_t \\ y_t \end{pmatrix} = \begin{pmatrix} A_x[2 \times 1] \\ A_y[1 \times 1] \end{pmatrix} + \begin{pmatrix} A_{xx}(L)[2 \times 2] & A_{xy}(L)[2 \times 1] \\ A_{yx}(L)[1 \times 2] & A_{yy}(L)[1 \times 1] \end{pmatrix} \begin{pmatrix} x_{t-1} \\ y_{t-1} \end{pmatrix} + \begin{pmatrix} e_{x,t} \\ e_{y,t} \end{pmatrix} \quad (4)$$

where  $A_x[2 \times 1]$  and  $A_y[1 \times 1]$  are two vectors of intercept terms,  $A_{xx}(L)[2 \times 2]$ ,  $A_{xy}(L)[2 \times 1]$ ,  $A_{yx}(L)[1 \times 2]$ , and  $A_{yy}(L)[1 \times 1]$  are matrices of lag polynomials,  $e_{x,t}$  and  $e_{y,t}$  are the corresponding error terms.

Testing the following null hypotheses:  $H_0^1: A_{xy}(L) = 0$  and  $H_0^2: A_{yx}(L) = 0$  is equivalent to testing the linear causality relationship between  $x_t$  and  $y_t$ . There are four different situations for the causality relationships between  $x_t$  and  $y_t$  in (1): (a) rejecting  $H_0^1$  but not rejecting  $H_0^2$  implies a unidirectional causality from  $y_t$  to  $x_t$ , (b) rejecting  $H_0^2$  but not rejecting  $H_0^1$  implies a unidirectional causality from  $x_t$  to  $y_t$ , (c) rejecting both  $H_0^1$  and  $H_0^2$  implies the existence of feedback relations, and (d) not rejecting both  $H_0^1$  and  $H_0^2$  implies that  $x_t$  and  $y_t$  are not rejected to be independent. Readers may refer to Bai, et al. (2010) for the details of testing  $H_0^1$  and/or  $H_0^2$ .

If the time series are cointegrated, one should impose the error-correction mechanism (ECM) on the VAR to construct a vector error correction model (VECM) in order to test Granger causality between the variables of interest. In particular, when testing the causality relationship between two vectors of non-stationary time series, we let  $\Delta x_t = (\Delta M_t, \Delta D_t)'$  and  $\Delta y_t = (\Delta Y_t)'$  be the corresponding stationary differencing series such that there are 3 series in total. If  $x_t$  and  $y_t$  are cointegrated, then instead of using the VAR in (1), one should adopt the following VECM model:

$$\begin{pmatrix} \Delta x_t \\ \Delta y_t \end{pmatrix} = \begin{pmatrix} A_x[2 \times 1] \\ A_y[1 \times 1] \end{pmatrix} + \begin{pmatrix} A_{xx}(L)[2 \times 2] & A_{xy}(L)[2 \times 1] \\ A_{yx}(L)[1 \times 2] & A_{yy}(L)[1 \times 1] \end{pmatrix} \begin{pmatrix} \Delta x_{t-1} \\ \Delta y_{t-1} \end{pmatrix} + \begin{pmatrix} \alpha_x[2 \times 1] \\ \alpha_y[1 \times 1] \end{pmatrix} \cdot ecm_{t-1} + \begin{pmatrix} e_{x,t} \\ e_{y,t} \end{pmatrix} \quad (5)$$

where  $ecm_{t-1}$  is lag one of the error correction term, and  $\alpha_x[2 \times 1]$  and  $\alpha_y[1 \times 1]$  are the coefficient vectors for the error correction term  $ecm_{t-1}$ . There are now two sources of causation of  $y_t(x_t)$  by  $x_t(y_t)$ , either through the lagged dynamic terms  $\Delta x_{t-1}(\Delta y_{t-1})$ , or through the error correction term  $ecm_{t-1}$ . Thereafter, one could test the null hypothesis  $H_0 : A_{xy}(L) = 0 (H_0 : A_{yx}(L) = 0)$  and/or  $H_0 : \alpha_x = 0 (H_0 : \alpha_y = 0)$  to identify Granger causality relation using the LR test.



## *Nonlinear Granger Causality*

Bai, et al. (2010, 2011, 2018) and Chow, et al. (2018) extend the nonlinear causality test developed by Hiemstra and Jones (1994) and others to the multivariate setting. To identify any nonlinear Granger causality relationship from any two series, say  $\{x_t\}$  and  $\{y_t\}$  in the bivariate setting, one has to first apply the linear model to  $\{x_t\}$  and  $\{y_t\}$  to identify their linear causal relationships and obtain the corresponding residuals,  $\{\hat{\varepsilon}_{1t}\}$  and  $\{\hat{\varepsilon}_{2t}\}$ . Thereafter, one has to apply a nonlinear Granger causality test to the residual series,  $\{\hat{\varepsilon}_{1t}\}$  and  $\{\hat{\varepsilon}_{2t}\}$ , of the two variables being examined to identify the remaining nonlinear causal relationships between their residuals. This is also true if one would like to identify the existence of any nonlinear Granger causality relation between two vectors of time series, say  $x_t = (x_{1,t}, \dots, x_{n_1,t})'$  and  $y_t = (y_{1,t}, \dots, y_{n_2,t})'$  in the multivariate setting. One has to apply the VAR model or the VECM model to the series to identify their linear causal relationships and obtain their corresponding residuals. Thereafter, one has to apply a nonlinear Granger causality test to the residual series. For simplicity, in this section we denote  $X_t = (X_{1,t}, \dots, X_{n_1,t})'$  and  $Y_t = (Y_{1,t}, \dots, Y_{n_2,t})'$  to be the corresponding residuals of any two vectors of variables being examined. We first define the lead vector and lag vector of a time series, say  $X_{i,t}$ , as follows: for

$X_{i,t}$ ,  $i = 1, 2$ , the  $m_{x_i}$ -length lead vector and the  $L_{x_i}$ -length lag vector of  $X_{i,t}$  are:

$$X_{i,t}^{m_{x_i}} \equiv (X_{i,t}, X_{i,t+1}, \dots, X_{i,t+m_{x_i}-1}), m_{x_i} = 1, 2, \dots, t = 1, 2, \dots,$$

$$\begin{aligned} X_{i,t-L_{x_i}}^{L_{x_i}} &\equiv (X_{i,t-L_{x_i}}, X_{i,t-L_{x_i}+1}, \dots, X_{i,t-1}), L_{x_i} = 1, 2, \dots, t \\ &= L_{x_i} + 1, L_{x_i} + 2, \dots, \end{aligned}$$

respectively. We denote  $M_x = (m_{x_1}, \dots, m_{x_{n_1}})$ ,  $L_x =$

$$(L_{x_1}, \dots, L_{x_{n_1}}), m_x = \max(m_{x_1}, \dots, m_{x_{n_1}}), \text{ and } l_x = \max(L_{x_1}, \dots, L_{x_{n_1}}).$$

The  $m_{y_i}$ -length lead vector,  $Y_{i,t}^{m_{y_i}}$ , the  $L_{y_i}$ -length lag vector,  $Y_{i,t-L_{y_i}}^{L_{y_i}}$ , of

$Y_{i,t}$ , and  $M_y, L_y, m_y$ , and  $l_y$  can be defined similarly.

Given  $m_x, m_y, L_x, L_y$ , and  $e > 0$ , we define the following four events:

$$\{\|X_t^{M_x} - X_s^{M_x}\| < e\} \equiv \{\|X_{i,t}^{M_{x_i}} - X_{i,s}^{m_{x_i}}\| < e, \text{ for any } i = 1, \dots, n_1\};$$

$$\begin{aligned} &\{\|X_{t-L_x}^{L_x} - X_{s-L_x}^{L_x}\| < e\} \\ &\equiv \{\|X_{i,t-L_{x_i}}^{L_{x_i}} - X_{i,s-L_{x_i}}^{L_{x_i}}\| < e, \text{ for any } i = 1, \dots, n_1\}; \end{aligned}$$

$$\begin{aligned} &\{\|Y_t^{M_y} - Y_s^{M_y}\| < e\} \\ &\equiv \{\|Y_{i,t}^{m_{y_i}} - Y_{i,s}^{m_{y_i}}\| < e, \text{ for any } i = 1, \dots, n_2\}; \text{ and} \end{aligned}$$

$$\begin{aligned} &\{\|Y_{t-L_y}^{L_y} - Y_{s-L_y}^{L_y}\| < e\} \\ &\equiv \{\|Y_{i,t-L_{y_i}}^{L_{y_i}} - Y_{i,s-L_{y_i}}^{L_{y_i}}\| < e, \text{ for any } i = 1, \dots, n_2\}; \end{aligned}$$

where  $\|\cdot\|$  denotes the maximum norm which is defined as  $\|X - Y\| = \max(|x_1 - y_1|, |x_2 - y_2|, \dots, |x_n - y_n|)$  for any two vectors  $X = (x_1, \dots, x_n)$  and  $Y = (y_1, \dots, y_n)$ . The vector series  $\{Y_t\}$  is said not to strictly Granger cause another vector series  $\{X_t\}$  if

$$\begin{aligned} &Pr\left(\|X_t^{M_x} - X_s^{M_x}\| < e \mid \|X_{t-L_x}^{L_x} - X_{s-L_x}^{L_x}\| < e, \|Y_{t-L_y}^{L_y} - Y_{s-L_y}^{L_y}\| < e,\right) \\ &= Pr\left(\|X_t^{M_x} - X_s^{M_x}\| < e \mid \|X_{t-L_x}^{L_x} - X_{s-L_x}^{L_x}\| < e\right) \end{aligned}$$

(6)

where  $\Pr(\cdot | \cdot)$  denotes conditional probability. Applying (6), one has to use the following test statistic to test for the nonlinear Granger causality:

$$\sqrt{n} \left( \frac{c_1(M_x+L_x, L_y, e, n)}{c_2(L_x, L_y, e, n)} - \frac{c_3(M_x+L_x, e, n)}{c_4(L_x, e, n)} \right) \quad (7)$$

Readers may refer to Bai, et al. (2010, 2011, 2018) and Chow, et al. (2018) for the details of the equation (7). Under this setting, Bai, et al. (2010, 2011) prove that to test the null hypothesis,  $H_0$ , that  $\{Y_{1,t}, \dots, Y_{n_2,t}\}$  does not strictly Granger cause  $\{X_{1,t}, \dots, X_{n_1,t}\}$ , under the assumptions that the time series  $\{X_{1,t}, \dots, X_{n_1,t}\}$  and  $\{Y_{1,t}, \dots, Y_{n_2,t}\}$  are strictly stationary, weakly dependent, and satisfy the mixing conditions stated in Denker and Keller (1983), if the null hypothesis,  $H_0$ , is true,

the test statistic defined in (7) is distributed as  $N\left(0, \sigma^2(M_x, L_x, L_y, e)\right)$ .

(8)

When the test statistic in (7) is too far away from zero, we reject the null hypothesis. Readers may refer to Bai, et al. (2010, 2011, 2018) and Chow, et al. (2018) for the details of the consistent estimator of the covariance matrix.

The nonlinear causality test has the ability to detect a nonlinear deterministic process which originally "looks" random. The nonlinear causality test is a complementary test for the linear causality test as linear causality tests could not detect nonlinear causal relationship while the nonparametric approach adopted in this paper can capture the nonlinear nature of the relationship among variables.

From literature we note an interest in analyzing the cross-correlation relationship. Podobnik and Stanley (2008) propose a detrended cross-correlation analysis (DXA) to investigate power-law cross-correlations between different simultaneously-recorded time series in the presence of non-stationarity. Podobnik, et al. (2009) introduce a joint stochastic process to model cross-correlations. In addition, using stock market returns from two stock exchanges in China, Ruan, et al. (2018) employ the MF-DCCA to investigate the non-linear cross-correlation between individual investor sentiment and Chinese stock market return. Zhang, et al. (2018) study the cross-correlations between Chinese stock markets and the other three stock markets. Xiong, et al. (2018) use a new policy uncertainty index to investigate the time-varying correlation between economic policy uncertainty and Chinese stock market returns. Wan and Wong (2001) develop a model to study the contagion effect. Cerqueti, et al. (2018) develop a model based on Mixed Poisson Processes to deal with the theme of contagion in financial markets. Wang, et al. (2018) propose a non-Markovian social contagion model in multiplex networks with inter-layer degree correlations to delineate the behavior of spreading, and develop an edge-based compartmental theory to describe the model. The nonlinear causality used in this paper could also be used to measure nonlinear cross-correlation to handle the nonlinear contagion effect. One could easily use or modify Equation (6) to deal with the nonlinear cross-correlation and the nonlinear contagion effect.

## References

- Adeyeye, P. O., Fapetub, O., Alukob, O.A., Migiyo, S.O. (2015). Does Supply-Leading Hypothesis hold in a Developing Economy? A Nigerian Focus: *Procedia Economics and Finance*, 30, 30 – 37.
- Ahmed, A., Mmolainyane, K. (2014). Financial integration, capital market development and economic performance: Empirical evidence from Botswana. *Economic Modelling*, 42, 1-14.
- Akbas, Y. (2015). Financial development and economic growth in emerging market: bootstrap panel causality analysis. *Theoretical & Applied Economics*, 22(3), 171-186.
- Al-Yousif, Y. (2012). Financial development and economic growth: Another look at the evidence from developing countries. *Review of Financial Economics*, 11 (2), 131-150.
- Anwar, S., Sun, S. (2011). Financial development, foreign investment and economic growth in Malaysia. *Journal of Asian Economics*, 22(4), 335-342.
- Baek, E., Brock, W. (1992). A general test for nonlinear Granger causality: Bivariate model. Iowa State University and University of Wisconsin at Madison Working Paper

- Bai, Z.D., Hui, Y.C., Jiang, D.D., Lv, Z.H., Wong, W.K., Zheng, S.R. (2018), A New Test of Multivariate Nonlinear Causality, *PLOS ONE*, forthcoming.
- Bai, Z., Wong, W. K., Zhang, B. (2010). Multivariate linear and nonlinear causality tests. *Mathematics and Computers in Simulation*, 81(1), 5-17.
- Bai, Z., Li, H., Wong, W. K., Zhang, B. (2011). Multivariate causality tests with simulation and Application. *Statistics and Probability Letters*, 81(8), 1063–1071.
- Bittencourt, M. (2012). Financial development and economic growth in Latin America: Is Schumpeter right? *Journal of Policy Modelling*, 34(3), 341-355.
- Bojanic, A. (2012). The impact of financial development and trade on the economic growth of Bolivia. *Journal of Applied Economics*, 15(1), 51-70.
- Bumann, S., Hermes, N., Lensink, R. (2013). Financial liberalization and economic growth: A meta-analysis. *Journal of International Money and Finance*, 33, 255-281.
- Caballero, J. (2015). Banking crises and financial integration: Insights from networks. *Journal of International Financial Markets, Institutions and Money*, 34, 127-146.
- Calderón, C., Liu, L. (2003). The direction of causality between financial development and economic growth. *Journal of Development Economics*, 72 (1), 321-334.



- Cerqueti, R., Fenga, L., Ventura, M. (2018). Does the U.S. exercise contagion on Italy? A theoretical model and empirical evidence. *Physica A: Statistical Mechanics and its Applications*, 499, 436-442.
- Chen, J., Quang, T. (2014). The impact of international financial integration on economic growth: New evidence on threshold effects. *Economic Modelling*, 42, 475-489.
- Chiang, C., Qiao, Z., Wong, W.K., (2009). New evidence on the relation between return volatility and trading volume. *Journal of Forecasting* 29(5), 502–515.
- Chiou-Wei, S. Z., Chen, C. F., Zhu, Z. (2008). Economic growth and energy consumption revisited—evidence from linear and nonlinear Granger causality. *Energy Economics*, 30(6), 3063-3076.
- Chow, S.C., Cunado, J., Gupta, R., Wong, W.K. (2018). Causal Relationships between Economic Policy Uncertainty and Housing Market Returns in China and India: Evidence from Linear and Nonlinear Panel and Time Series Models, *Studies in Nonlinear Dynamics and Econometrics*, forthcoming.
- Deltuvaitė, V., Sinevičienė, L. (2014). Investigation of relationship between financial and economic development in the EU countries. *Procedia Economics and Finance*, 14, 173-180.
- Demetriades, P., Hussein, K. (1996). Does financial development cause economic growth? Time-series evidence from 16 countries. *Journal of development Economics*, 51(2), 387-411.

- Engle, R. F., & Granger, C. W. (1987). Co-integration and error correction: representation, estimation, and testing. *Econometrica: journal of the Econometric Society*, 251-276.
- Fan, J.J., Xu, R., Su, C.W., Shi, Q.H. 2018, Demand-following or supply-leading? Trade openness and financial development in China, *Journal of International Trade & Economic Development*, 27(3), 314-332.
- Fomby, T., Hill, R., Johnson, S. (2012). *Advanced econometric methods*. Springer Science & Business Media.
- Gelb, A. H. (1989). *Financial policies, growth, and efficiency* (Vol. 202). World Bank Publications.
- Granger, C. W. J. (2014). *Forecasting in business and economics*. Academic Press.
- Gonzalo, J. (1994). Five alternative methods of estimating long-run equilibrium relationships. *Journal of econometrics*, 60(1-2), 203-233.
- Goldsmith, R. (1969). *Financial structure and development*. New Haven, CT: Yale U. Press.
- Gregorio, J., Guidotti, P. (1995). Financial development and economic growth. *World Development*, 23(3), 433-448.
- Hamilton, J. D. (2011). Nonlinearities and the macroeconomic effects of oil prices. *Macroeconomic dynamics*, 15(S3), 364-378.
- Hassan, M., Sanchez, B., Yu, J. (2011). Financial development and economic growth: New evidence from panel data. *Quarterly Review of Economics and Finance*, 51 (1), 88–104

- Herrera, A. M., Lagalo, L. G., Wada, T. (2011). Oil price shocks and industrial production: Is the relationship linear?. *Macroeconomic Dynamics*, 15(S3), 472-497.
- Herwartz, H., Walle, Y. (2014). Determinants of the link between financial and economic development: Evidence from a functional coefficient model. *Economic Modelling*, 37, 417-427.
- Hiemstra, C., Jones, J. (1994). Testing for linear and nonlinear Granger causality in the stock price-volume relation. *Journal of Finance*, 49(5), 1639-1664.
- Horng, M.S., Chang, Y.W., Wu, T.Y. (2012). Does insurance demand or financial development promote economic growth? Evidence from Taiwan. *Applied Economics Letters*, 19(2), 105-111.
- Hsueh, S., Hu, Y., Tu, C. (2013). Economic growth and financial development in Asian countries: A bootstrap panel Granger causality analysis, *Economic Modelling*, 32, 294-301.
- Hui, Y.C., Wong, W.K., Bai, Z.D., Zhu, Z.Z. (2017). A New Nonlinearity Test to Circumvent the Limitation of Volterra Expansion with Application, *Journal of the Korean Statistical Society*, 46(3), 365-374.
- Jedidia, K., Boujelbène, T., Helali, K. (2014). Financial development and economic growth: New evidence from Tunisia. *Journal of Policy Modelling*, 36(5), 883-898.
- Johansen, S. (1988). Statistical analysis of cointegration vectors. *Journal of economic dynamics and control*, 12(2-3), 231-254.

- Johansen, S. (1991), Estimation and Hypothesis Testing of Cointegration Vectors in Gaussian Vector Autoregressive Models, *Econometrica*, 59(6), 1551–1580.
- Johansen, S., & Juselius, K. (1990). Maximum likelihood estimation and inference on cointegration—with applications to the demand for money. *Oxford Bulletin of Economics and statistics*, 52(2), 169-210.
- Kar, M., Nazlıoğlu, S., Ağır, H. (2011). Financial development and economic growth nexus in the MENA countries: Bootstrap panel granger causality analysis. *Economic Modelling*, 28 (1–2), 685-693.
- King, R., Levine, R. (1993). Finance and growth: Schumpeter might be right. *Quarterly Journal of Economics*, 108(3), 717-737.
- Khan, A. (2001). Financial development and economic growth. *Macroeconomic dynamics*, 5(3), 413-433.
- Lee, T. H., & Tse, Y. (1996). Cointegration tests with conditional heteroskedasticity. *Journal of Econometrics*, 73(2), 401-410.
- Levine, R. (1997). Financial development and economic growth: views and agenda. *Journal of economic literature*, 35(2), 688-726.
- Menyah, K., Nazlioglu, S., Wolde-Rufael, Y. (2014). Financial development, trade openness and economic growth in African countries: New insights from a panel causality approach. *Economic Modelling*, 37, 386-394.

- Murinde, V., Eng, F.S.H. (1994). Financial development and economic growth in Singapore: demand-following or supply-leading?, *Applied Financial Economics*, 4(6), 391-404.
- Narayan, P., Narayan, S. (2013). The short-run relationship between the financial system and economic growth: New evidence from regional panels. *International Review of Financial Analysis*, 29, 70-78.
- Ngare, E, Nyamongo, E., Misati, R. (2014). Stock market development and economic growth in Africa. *Journal of Economics and Business*, 74, 24-39.
- Owyong, D., Wong, W.K., Horowitz, I. 2015, Cointegration and Causality among the Onshore and Offshore Markets for China's Currency, *Journal of Asian Economics* 41, 20-38.
- Patrick, H. (1966). Financial development and economic growth in underdeveloped countries. *Economic development and Cultural change*, 14(2), 174-189.
- Podobnik, B., Horvatic, D., Petersen, A., Stanley, H.E. (2009). Cross-Correlations between Volume Change and Price Change, *Proceedings of the National Academy of Sciences of the USA*, 106:22079-22084.
- Podobnik, B., Stanley, H.E. (2008). Detrended Cross-Correlation Analysis: A New Method for Analyzing Two Non-stationary Time Series, *Physical Review Letters*, 100(8), 084102.

- Qiao, Z., Li, Y., Wong, W.K. (2008). Policy change and lead–lag relations among China’s segmented stock markets, *Journal of Multinational Financial Management*, 18, 276–289.
- Qiao, Z., McAleer, M., Wong, W.K. (2009). Linear and nonlinear causality of consumption growth and consumer attitudes, *Economics Letters*, 102(3), 161–164.
- Rehman, M.U. (2017). Do oil shocks predict economic policy uncertainty?. *Physica A: Statistical Mechanics and its Applications*, 498, 123-136.
- Robinson, J. (1952). The generalization of the general theory, In: the rate of interest and other essays, London: MacMillan.
- Roubini, N., Sala-i-Martin, X. (1992). Financial repression and economic growth. *Journal of Development Economics*, 39(1), 5-30.
- Ruan, Q., Yang, H., Lv, D., Zhang, S. (2018). Cross-correlations between individual investor sentiment and Chinese stock market return: New perspective based on MF-DCCA. *Physica A: Statistical Mechanics and its Applications*, 503, 243-256.
- Samargandi, N., Fidrmuc, J., Ghosh, S. (2015). Is the relationship between financial development and economic growth monotonic? Evidence from a sample of middle-income countries. *World Development*, 68, 66-81.
- Schumpeter, J. A. (1934). *Capitalism, socialism and democracy*. Routledge.

- Schumpeter, J., Backhaus, U. (2003). The theory of economic development. In *Joseph Alois Schumpeter* (pp. 61-116). Springer US.
- Uddin, G., Sjö, B., Shahbaz, M. (2013). The causal nexus between financial development and economic growth in Kenya. *Economic Modelling*, 35, 701–707.
- Valickova, P., Havranek, T., Horvath, R. (2015). Financial Development and Economic Growth: A Meta-Analysis. *Journal of Economic Surveys*, 29(3), 506-526.
- Wan, H.Jr, Wong, W.K. (2001). Contagion or inductance? Crisis 1997 reconsidered, *Japanese Economic Review*, 52(4), 372-380.
- Wang, W., Cai, M., Zheng, M. (2018). Social contagions on correlated multiplex networks. *Physica A: Statistical Mechanics and its Applications*, 499, 436-442.
- Xiong, X., Bian, Y., Shen, D. (2018). The time-varying correlation between policy uncertainty and stock returns: Evidence from China. *Physica A: Statistical Mechanics and its Applications*, 499, 413-419.
- Yang, Y., Yi, M. (2008). Does financial development cause economic growth? Implication for policy in Korea. *Journal of Policy Modelling*, 30(5), 827-840.
- Zhang, J., Wang, L., Wang, S. (2012). Financial development and economic growth: Recent Evidence from China. *Journal of Comparative Economics*, 40 (3), 393-412.

Zhang, X., Zhu, Y., Yang, L. (2018). Multifractal detrended cross-correlations between Chinese stock market and three stock markets in The Belt and Road Initiative. *Physica A: Statistical Mechanics and its Applications*, forthcoming.